



COMPRESSIBILITY COEFFICIENT

INTRODUCTION

The ratio of the mean airflow rate through the fan to the airflow rate at fan air density; the ratio of the fan total pressure that would be developed with an incompressible fluid to the fan total pressure that is developed with a compressible fluid, i.e., air, the test gas.

The compressibility coefficient is a thermodynamic factor that must be applied to determine fan total efficiency from fan airflow rate, fan total pressure, and fan input power.

Note: Where the fan total efficiency is less than or equal to $(\gamma-1)/\gamma$, assume $K_p = 1$.

English (IP) Units of Measure:

$$x = \frac{P_t}{P_{t1} + 13.595(p_b)}$$

$$z = \left(\frac{\gamma - 1}{\gamma}\right) \left(\frac{6343.3 \left(\frac{H}{Q}\right)}{P_{t1} + 13.595(p_b)}\right)$$

$$K_p = \left(\frac{\ln(1 + x)}{x}\right) \left(\frac{z}{\ln(1 + z)}\right)$$

Metric (SI) Units of Measure:

$$x = \frac{P_t}{P_{t1} + p_b}$$

$$z = \left(\frac{\gamma - 1}{\gamma}\right) \left(\frac{1000 \left(\frac{H}{Q}\right)}{P_{t1} + p_b}\right)$$

$$K_p = \left(\frac{\ln(1 + x)}{x}\right) \left(\frac{z}{\ln(1 + z)}\right)$$

THE FAN COMPRESSIBILITY RATIO (K_P/K_{PC}) IS CALCULATED AS FOLLOWS:

English (IP) Units of Measure:

$$\frac{z}{z_c} = \frac{13.595p_{bc} + P_{t1c}}{13.595p_b + P_{t1}} \times \frac{\rho}{\rho_c} \times \left(\frac{N}{N_c}\right)^2 \times \left(\frac{D}{D_c}\right)^2 \times \frac{\gamma_c}{\gamma_c - 1} \times \frac{\gamma - 1}{\gamma}$$

$$z_c = \frac{z}{z/z_c}$$

$$\ln(1 + x_c) = \ln(1 + x) \left(\frac{\ln(1 + z_c)}{\ln(1 + z)}\right) \left(\frac{\gamma - 1}{\gamma}\right) \left(\frac{\gamma_c}{\gamma_c - 1}\right)$$

$$x_c = e^{\ln(1+x_c)} - 1$$

$$\frac{K_p}{K_{pc}} = \left(\frac{z}{z_c}\right) \left(\frac{x_c}{x}\right) \left(\frac{\gamma}{\gamma - 1}\right) \left(\frac{\gamma_c - 1}{\gamma_c}\right)$$

Metric (SI) Units of Measure:

$$\frac{z}{z_c} = \left(\frac{p_{bc} + P_{t1c}}{p_b + P_{t1}}\right) \left(\frac{\rho}{\rho_c}\right) \left(\frac{N}{N_c}\right)^2 \left(\frac{D}{D_c}\right)^2 \left(\frac{\gamma_c}{\gamma_c - 1}\right) \left(\frac{\gamma - 1}{\gamma}\right)$$

$$z_c = \frac{z}{z/z_c}$$

$$\ln(1 + x_c) = \ln(1 + x) \left(\frac{\ln(1 + z_c)}{\ln(1 + z)}\right) \left(\frac{\gamma - 1}{\gamma}\right) \left(\frac{\gamma_c}{\gamma_c - 1}\right)$$

$$x_c = e^{\ln(1+x_c)} - 1$$

$$\frac{K_p}{K_{pc}} = \left(\frac{z}{z_c}\right) \left(\frac{x_c}{x}\right) \left(\frac{\gamma}{\gamma - 1}\right) \left(\frac{\gamma_c - 1}{\gamma_c}\right)$$

**CALCULATE CONVERTED (FULL SIZE) FAN PERFORMANCE
FROM BASELINE (MODEL) VALUES PER:**

$$\begin{aligned}Q_c &= Q \times (D_c/D)^3 \times (N_c/N) \times (K_p/K_{pc}) \\P_{tc} &= P_t \times (D_c/D)^2 \times (N_c/N)^2 \times (\rho_c/\rho) \times (K_p/K_{pc}) \\P_{vc} &= P_v \times (D_c/D)^2 \times (N_c/N)^2 \times (\rho_c/\rho) \\P_{sc} &= P_{tc} - P_{vc} \\H_c &= H \times (D_c/D)^5 \times (N_c/N)^3 \times (\rho_c/\rho) \times (K_p/K_{pc}) \\\eta_{sc} &= \eta_{tc} \times (P_{sc}/P_{tc}) \\\eta_{tc} &= \eta_t\end{aligned}$$

Where:

D_c	=	full size impeller diameter
D	=	model fan impeller diameter
P_{tc}	=	full size fan total pressure
P_t	=	model fan total pressure
P_{sc}	=	full size fan static pressure
P_s	=	model fan static pressure
P_{vc}	=	full size fan velocity pressure
P_v	=	model fan velocity pressure
Q_c	=	full size fan airflow rate
Q	=	model fan airflow rate
N_c	=	full size fan rotational speed
N	=	model fan rotational speed
ρ_c	=	full size fan air density
ρ	=	model fan air density
H_c	=	full size fan power
H	=	model fan power
K_{pc}	=	full size fan compressibility coefficient
K_p	=	model fan compressibility coefficient
η_{tc}	=	full size fan total efficiency
η_{sc}	=	full size fan static efficiency

Units:

Symbol	Description	English (IP) Unit	Metric (SI) Unit
Subscript C	Denotes corrected value	N/A	N/A
D	Diameter	inches	mm
H	Fan power	hp	kW
K _P	Compressibility coefficient	Dimensionless	Dimensionless
N	Rotational speed	rpm	rpm
P _s	Fan static pressure	in. wg	Pa
P _t	Fan total pressure	in. wg	Pa
P _{t1}	Total pressure at inlet plane	in. wg	Pa
P _V	Fan velocity pressure	in. wg	Pa
Q	Fan airflow rate	ft ³ /min	m ³ /s
γ	Specific heat ratio	Dimensionless	Dimensionless
ρ	Fan air density	lbm/ft ³	kg/m ³
P _b	Barometric pressure	In. Hg	Pa
η _t	Fan total efficiency	Per unit	Per unit
η _s	Fan static efficiency	Per unit	Per unit